

# Diagnosis, Device Placement, and Auxiliary Control for Resilience

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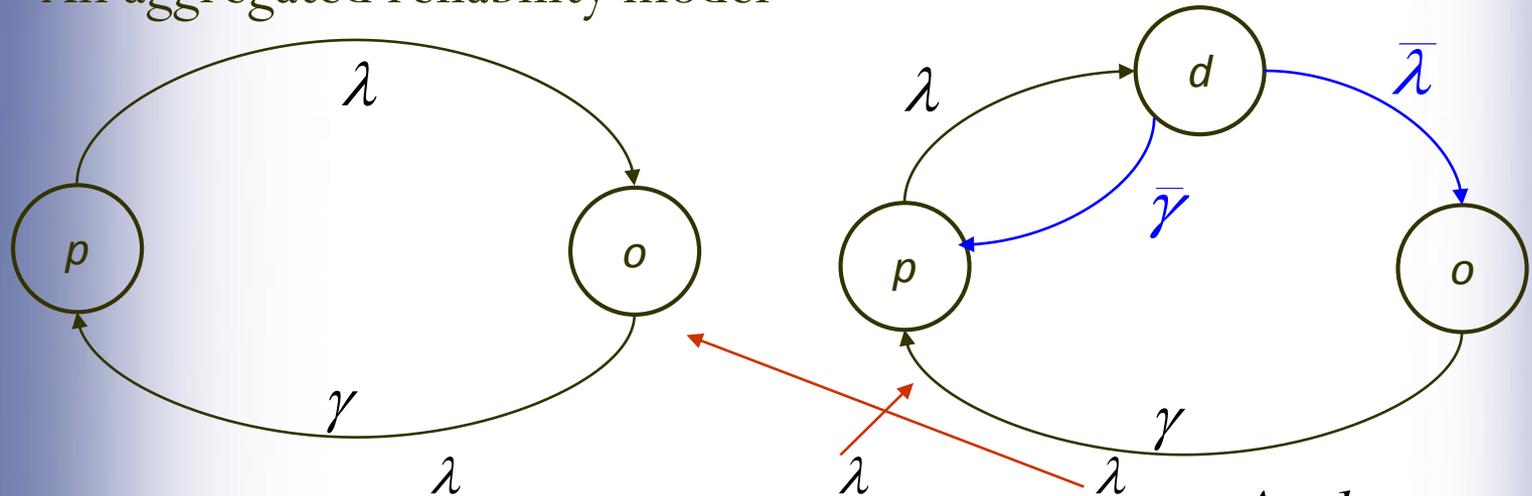
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Reliability of power systems:  
ability to provide uninterrupted service: adequacy (availability)  
and ability to withstand disturbances: **security** (transient stability)

- Protection misoperations
  - Failure to trip, false trip
  - 1965 NE, 2003 NE, 2011 SW blackouts
- Challenges
  - Rare/high impact events costly to prevent and costly not to prevent
  - Response speed required of protection functions
- Objective
  - Introduce a framework that enables us to formally address the challenges and examine the technology readiness

# What makes the gird more reliable?

- An aggregated reliability model

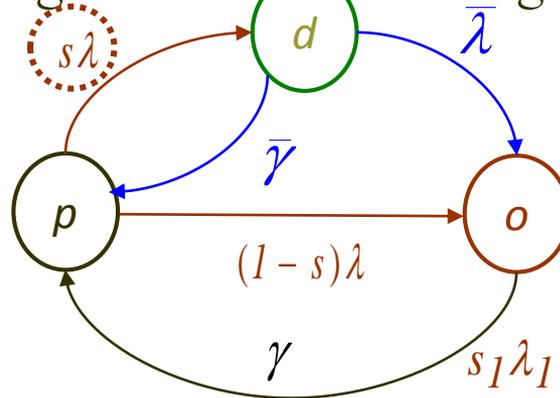
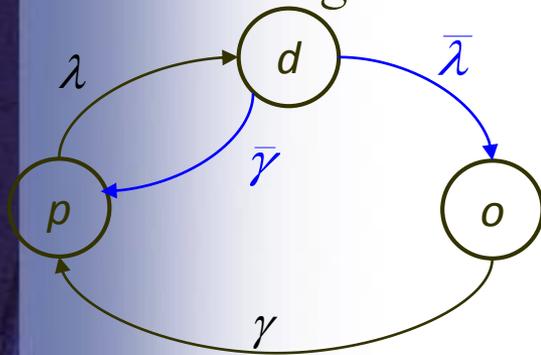


$$\pi_o = \frac{\lambda}{\lambda + \gamma + (\lambda + \bar{\gamma})\gamma / \bar{\lambda}} \cong \frac{\lambda}{\lambda + \gamma + \gamma\bar{\gamma} / \bar{\lambda}} < \frac{\lambda}{\lambda + \gamma}, \quad A = 1 - \pi_o$$

- Reliability benefits greatly from **diverting** all critical faults to state  $d$ , at which a more expeditious recovery to normal from the degraded state (N-1 secure)
- Assumption: protection is perfect
  - How to quantify the imperfection?

## Introducing security index

- $s$ : security (conditional probability of successful transition into the degraded state given event of leading to the transition)

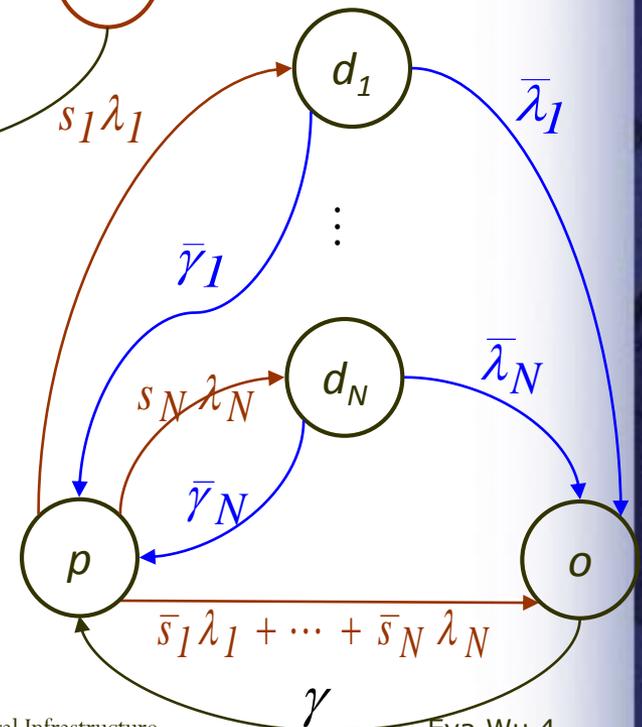


- Expansibility

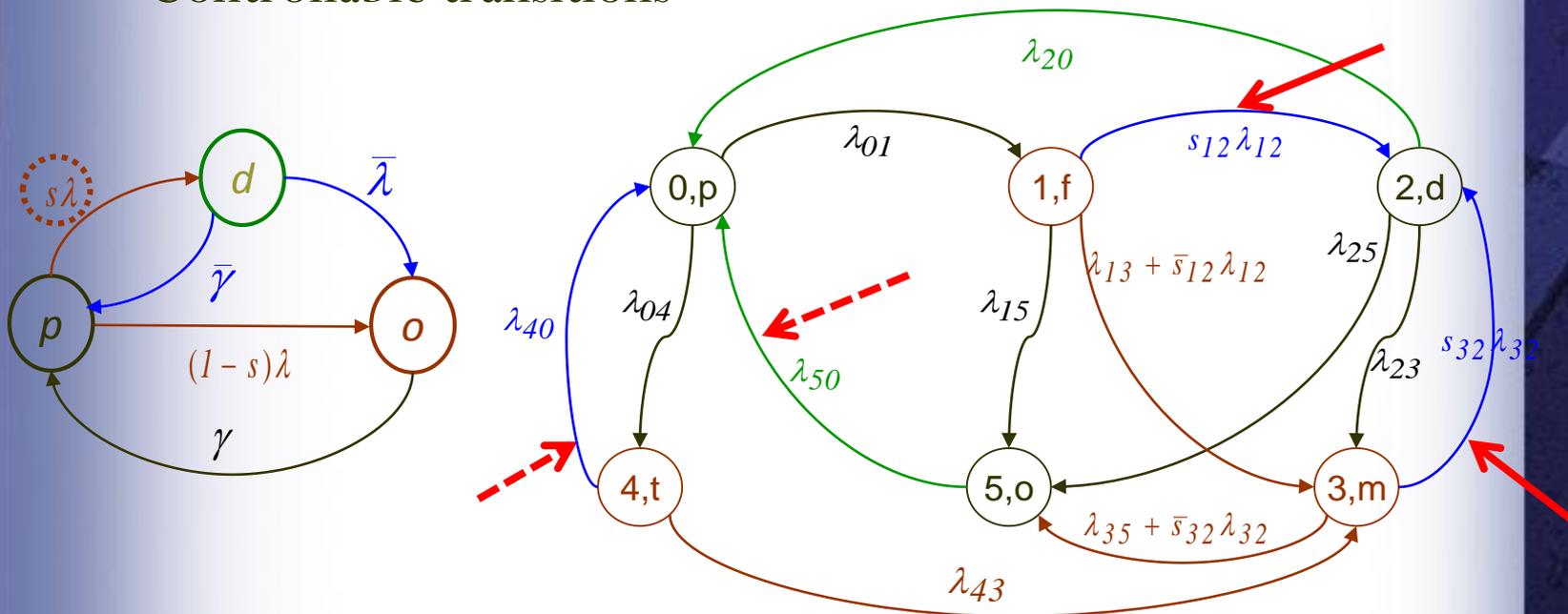
- Modes  $\{f_0, f_1, \dots, f_N, f_{N+1}, \}$

- Scalability - linear w.r.t. system size

- Evaluation of  $S_i$ ?



- Inclusion of insecure states in order to develop auxiliary control
  - Pre-fault state is split to include an aggregated false trip state
  - Degraded state is split to include an aggregated fault-on state
  - Outage state is split to include an aggregated misoperated state with fault-on
  - Controllable transitions



Security of controllable transitions

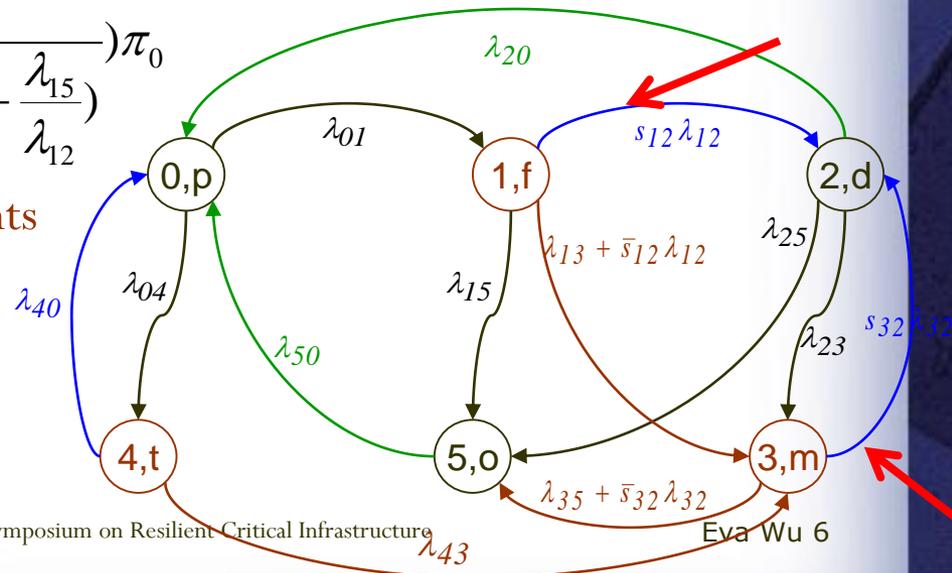
- $s_{ij} = c_{ij}p_{ij}$ 
  - conditional probability of correct mode identification
  - conditional probability of correct control action)
- Control and diagnosis risks (Poisson decomposition)
- Event probability, availability

$$P[2 | 1] \cong s_{12}$$

$$P[2 | 3] \cong s_{32}$$

$$A_s \cong 1 - \frac{\lambda_{01}}{\lambda_{05}} \left( 1 - \frac{s_{32}\bar{s}_{12} + s_{12}}{\left(1 + \frac{\lambda_{25} + \bar{s}_{32}\lambda_{23}}{\lambda_{20}}\right)\left(1 + \frac{\lambda_{15}}{\lambda_{12}}\right)} \right) \pi_0$$

Technological requirements



- Auxiliary control criterion
  - Estimated post-fault stability region in a physical state space based on the system energy function established by protective control action  $u$  exerted at time  $t$
  - Estimated fault-on physical state at the time  $t$  that has a probability called a fault-coverage of being in the post-fault stability region.

Characteristic function  
in product space  $(x, t)$

$$c_{i,u}(t) = \int_{x,t} \overbrace{J_{i,u}(x,t)} \underbrace{f(\hat{x}, \hat{t}_0)(t, x, t_0)}_{\text{Joint distribution of state, fault onset time}} dx dt$$

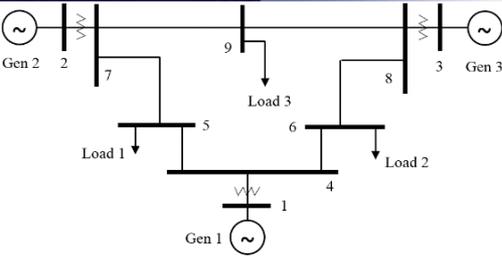
- Diagnosis criterion
  - A conditional probability simplex (conditioned on knowledge of the protective control action  $u$ ) in an  $N+1$  dimensional information space
  - Estimated information state, representing system mode probability distribution at time  $t$

$$p_{f_i}(t_k) = \frac{p_{f_i}(t_{k-1})\rho_{\xi_{f_i}}(t_k)}{\sum_j p_{f_j}(t_{k-1})\rho_{\xi_{f_j}}(t_k)}$$

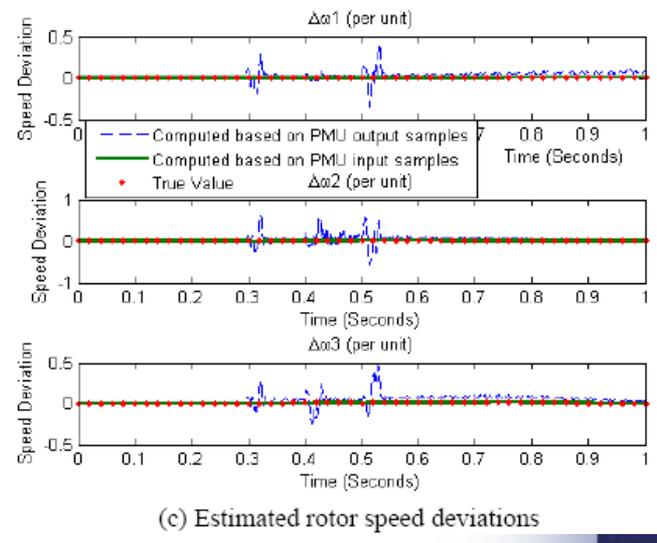
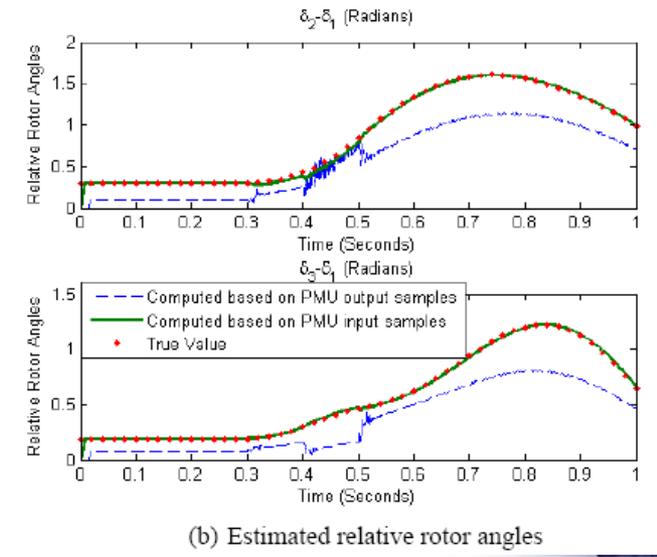
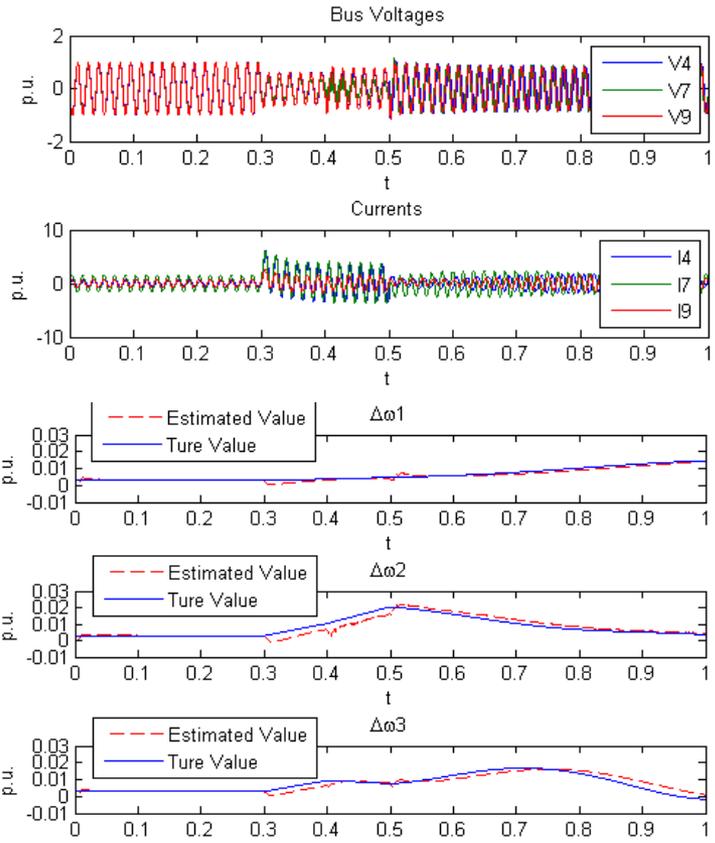
Probability of model matching

# Example: security profiles of a 9-bus system

- PMU-based in electromechanical state tracking
  - Input samples at 24 samples/cycle
  - No swing dynamics involved



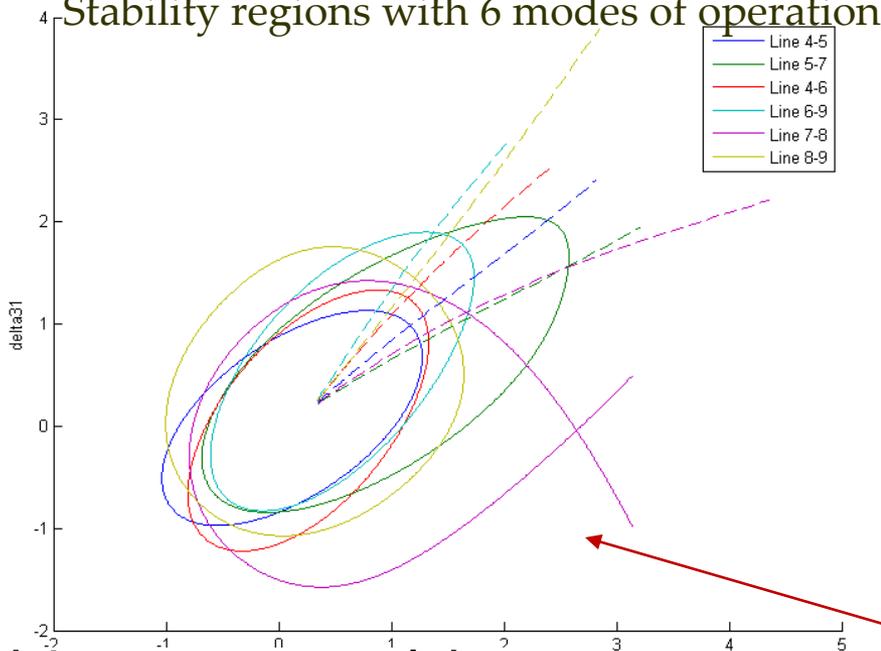
6 transmission line faults considered  
3 PMU-like sensors at buses 4, 7, and 9



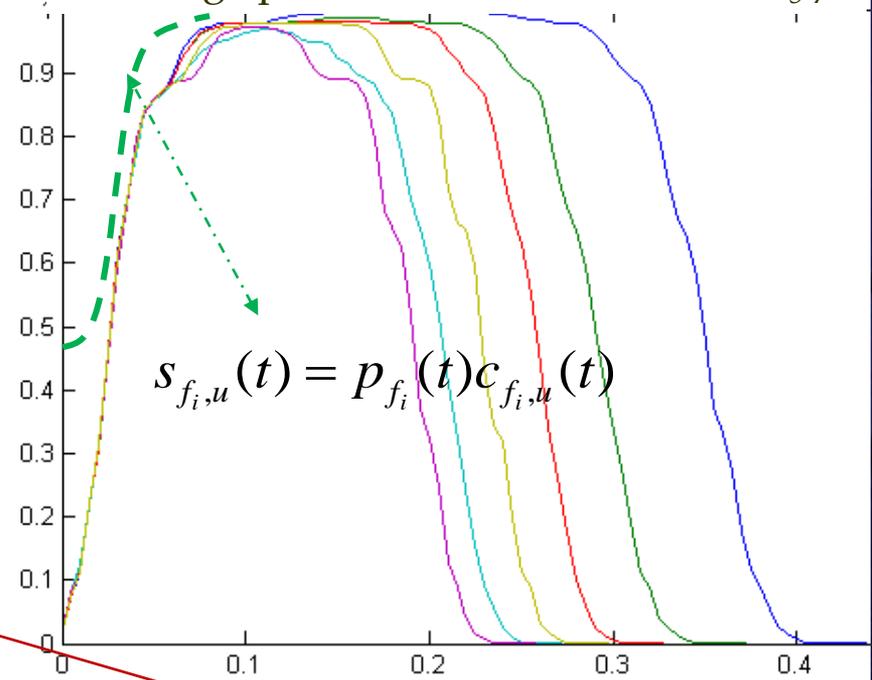
$$c_{i,u}(t) = \int_{x,t} J_{i,u}(x,t) f(\hat{x}, \hat{t}_0)(t, x, t_0) dx dt_0$$

- PMU-aided auxiliary control
  - Bad news: diagnosis necessary
  - Good news: opportunity for recovery from protection misoperation

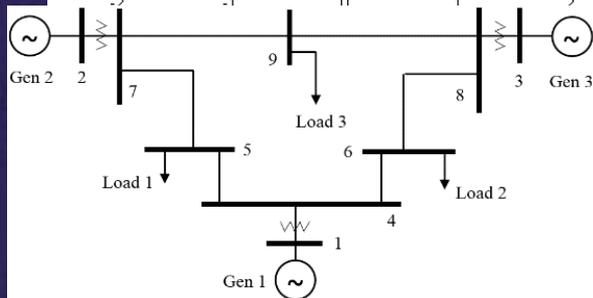
Stability regions with 6 modes of operation



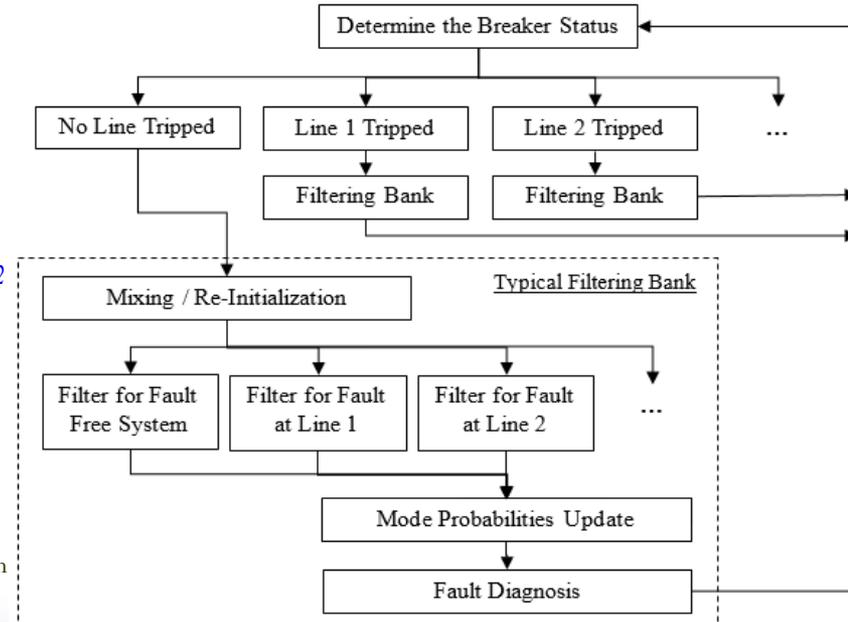
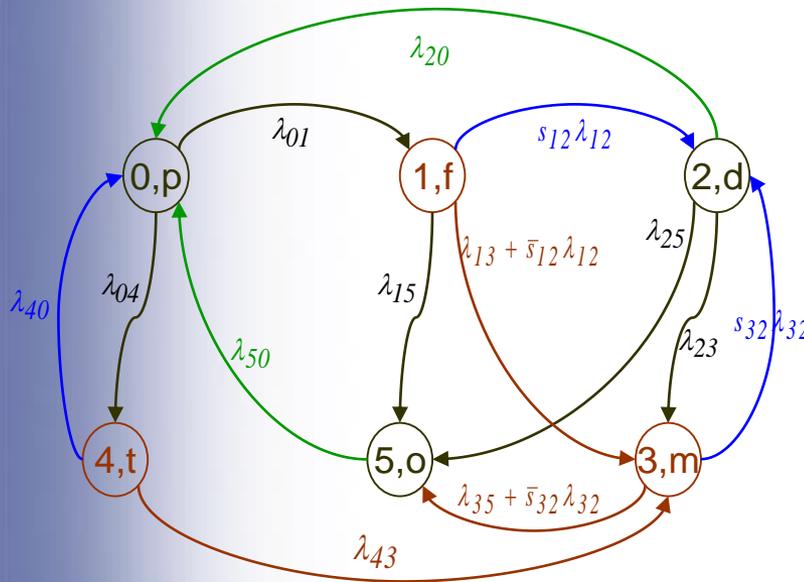
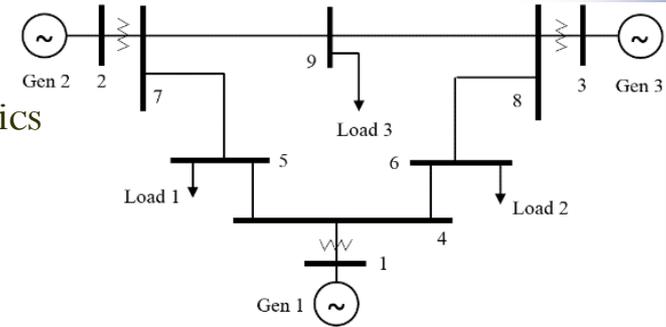
Coverage profiles evaluated over  $RoA_{5-7}$



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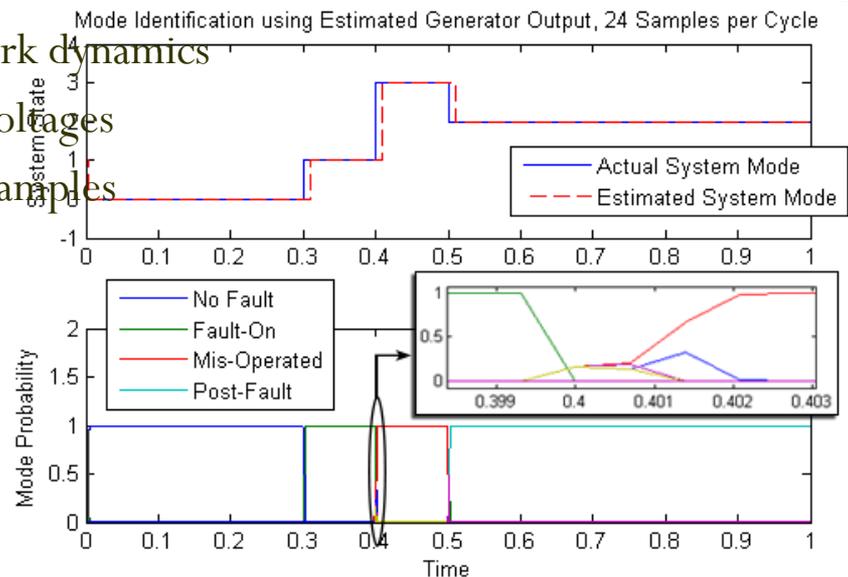
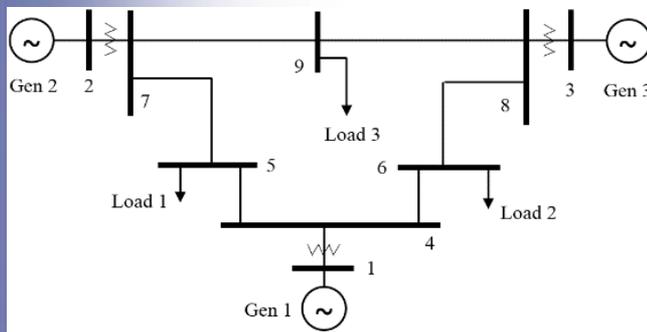


- Computing mode probability
  - Diagnosis to identify which equipment should be removed in the face of protection misoperations
    - A bank of filters are designed for each known state of protection system
  - Use of PMU-like sensors
    - Filters built on electric network dynamics
    - Inputs: estimated generator voltages
    - Outputs: other sensor input samples



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### Desired secondary protection functions

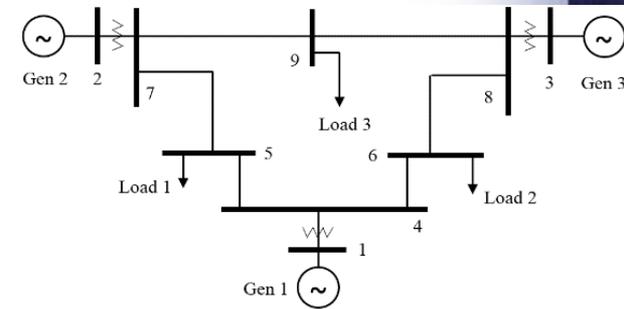
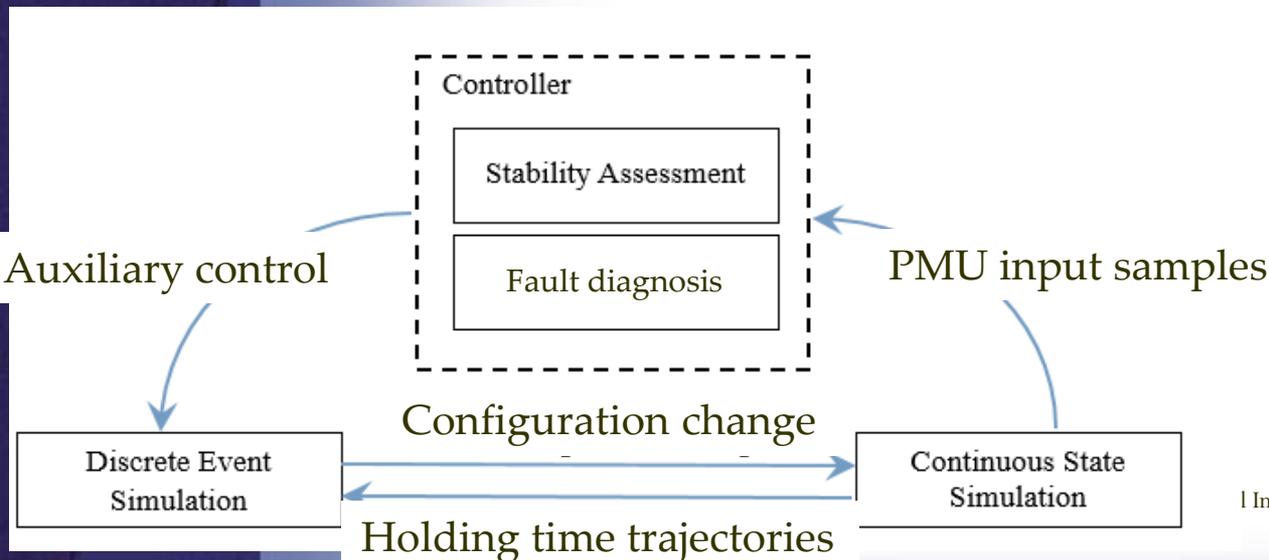
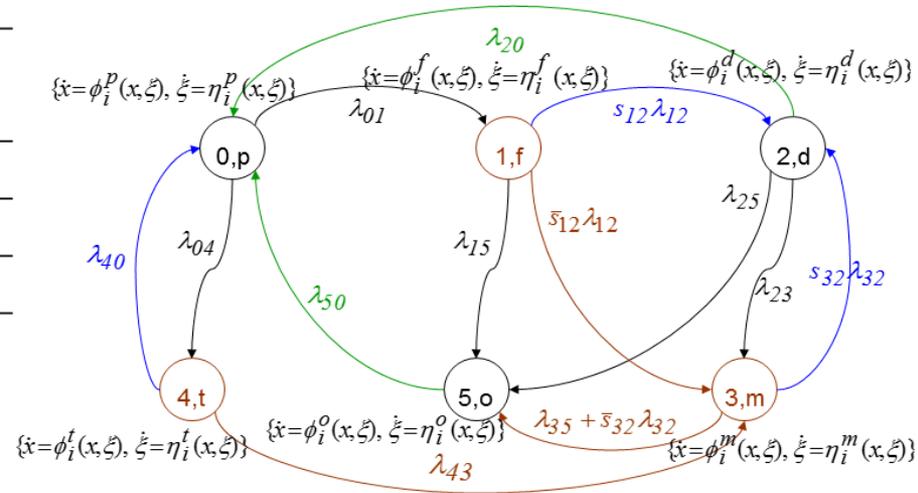
True mode	Identified mode by primary protection	Control action by secondary protection
$f_i$	$f_i$	no action
$f_i, i > 0$	$f_0$	recover from failure to trip
$f_i,$	$f_j, j \neq i$	recover from false trip

## Assumptions

- Short-to ground uniformly distributed along transmission
- Single representative fault-on model/line

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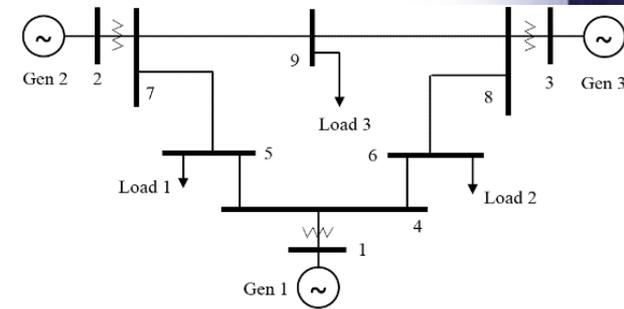
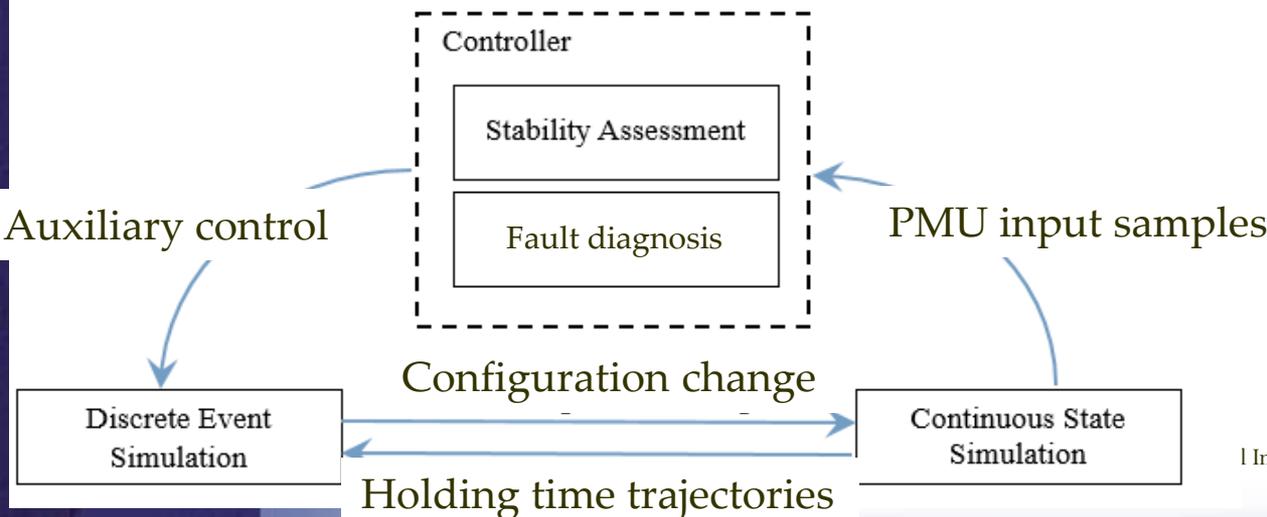
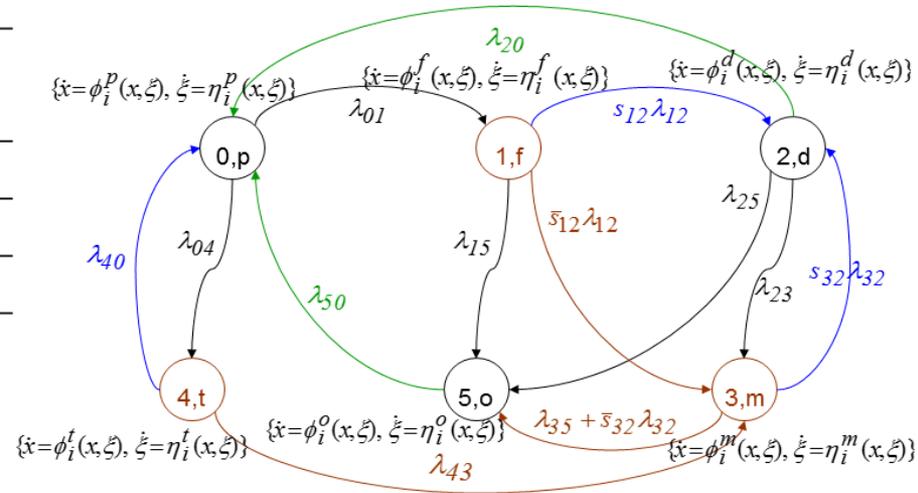


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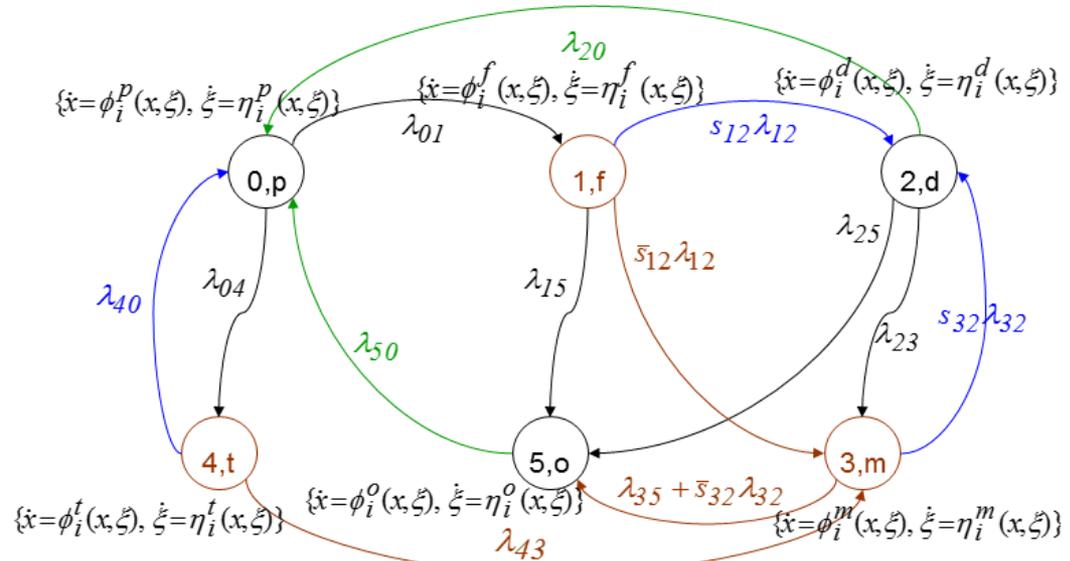
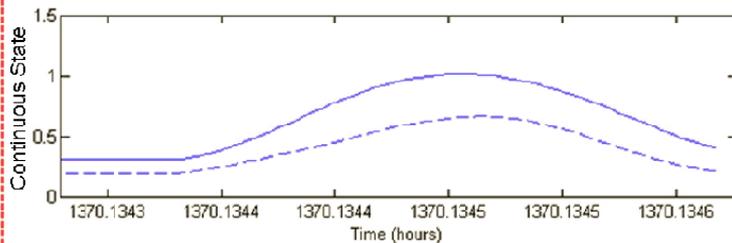
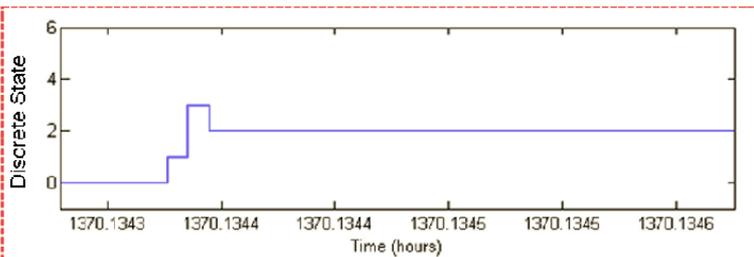
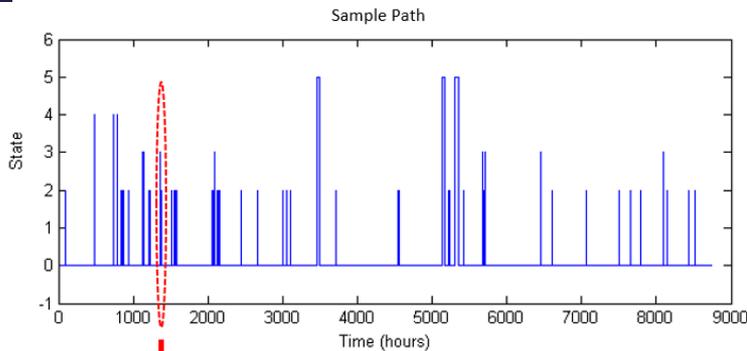
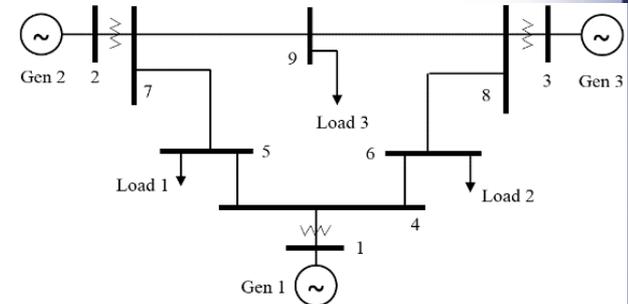
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- Steady-state probability and event probability

	$\pi_0$	$\pi_2$	$\pi_5$	$Prob[d m]$
w/o secondary protect.	0.9425	0.0165	0.0406	0.0000
w/ secondary protect.	0.9643	0.0212	0.0137	0.4024



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